
1st PRISMA Interactive Research Symposium

Precise Standard Model predictions for the Mu3e and MEG experiment

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21ST FEBRUARY 2017

Motivation

The radiative decay (MEG)

The rare decay ($\text{Mu}3e$)

Outlook

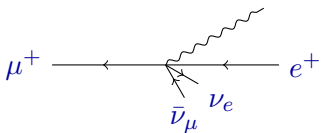
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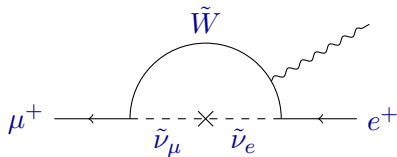
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Importance of background



Radiative decay
 $(\mu \rightarrow \nu \bar{\nu} e + \gamma)$
 $E_{\nu \bar{\nu}} < \Delta E_{\text{exp.}}$



LFV decay
 $(\mu \rightarrow e \gamma)$

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Radiative $\mu \rightarrow \nu \bar{\nu} e + \gamma$	MEG $\mathcal{O}(1\%)$	NLO (polarised, MC) [?] [?]
Rare $\mu \rightarrow \nu \bar{\nu} e + e^+ e^-$	Mu3e $\mathcal{O}(10\%)$	NLO (polarised, MC) [?] [?]

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- NEW: NLO for rare decay

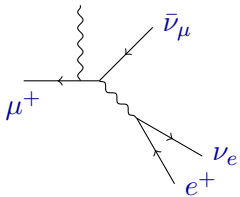
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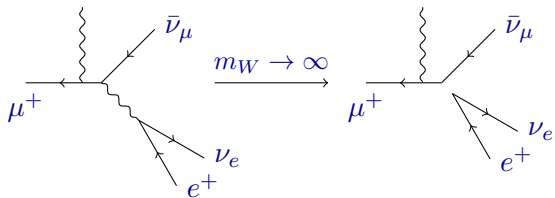
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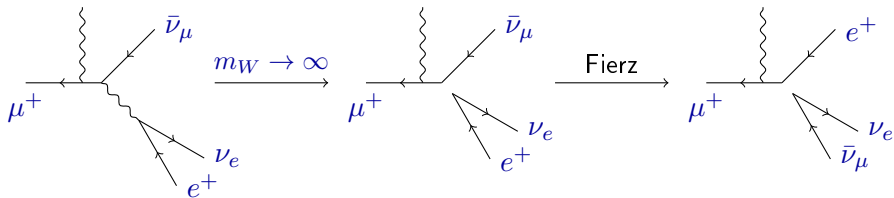
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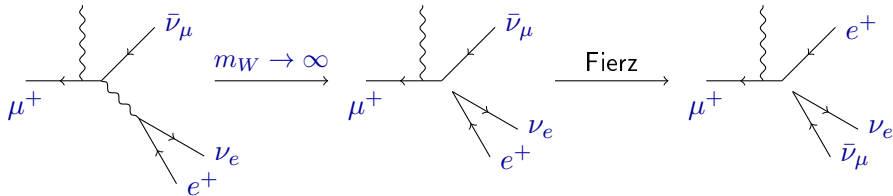


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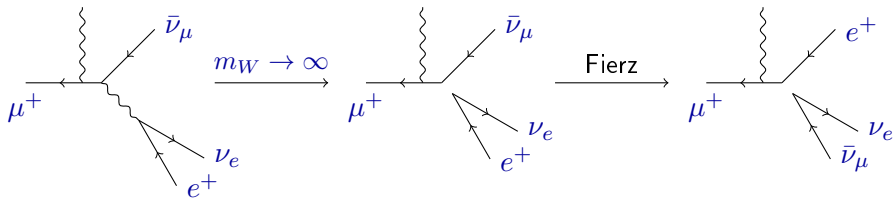
The radiative decay





- 4-Fermi interaction, fierzied at the Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{QED}} + \frac{G_F}{\sqrt{2}} j_{V-A}(\mu, e) \cdot j_{V-A}(\nu_\mu, \nu_e)$$



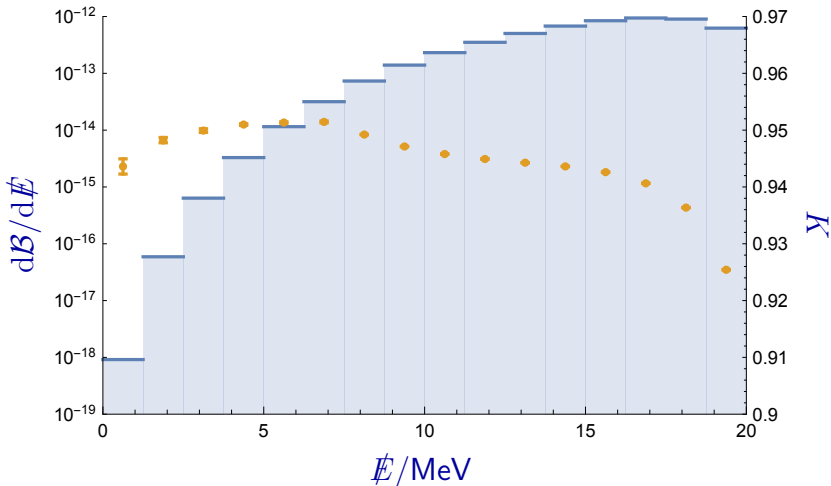
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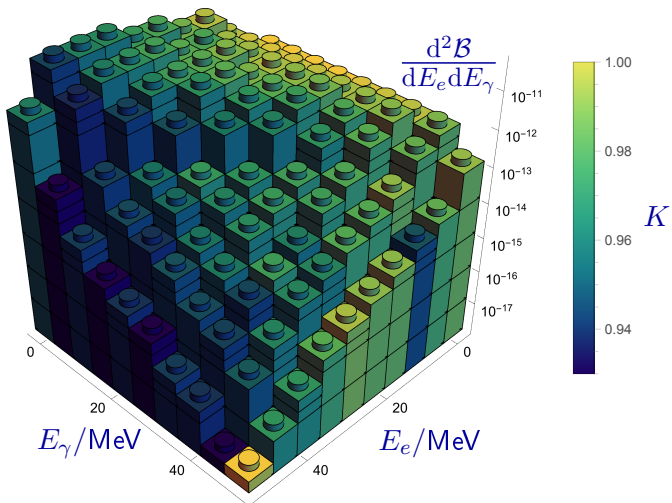
- GoSam [?] / FKS subtraction [?] / VEGAS [?]

Invisible energy spectrum

- Using theorist's MEG cuts



Double differential energy distribution

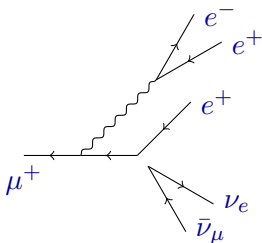


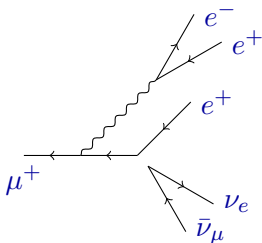
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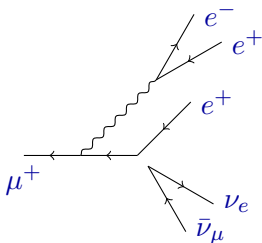
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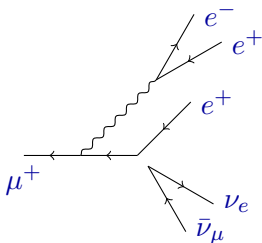




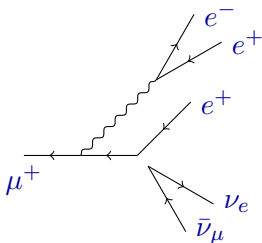
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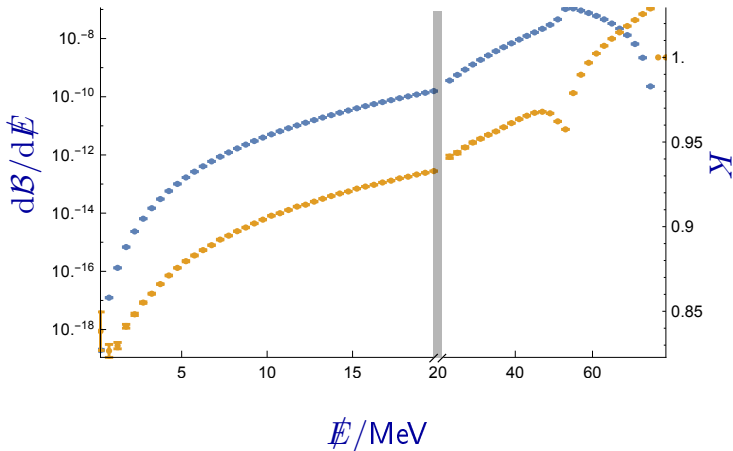


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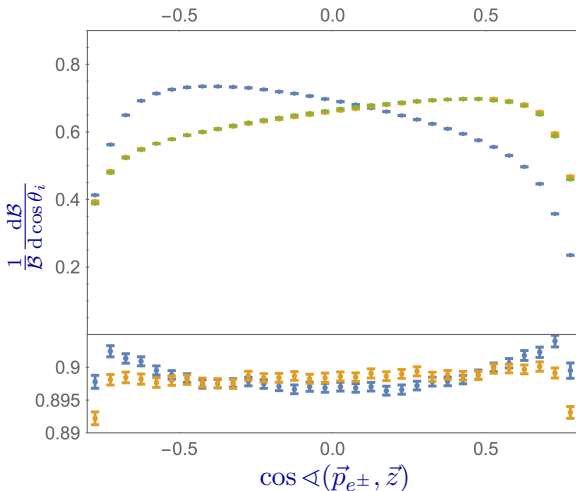
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- Use same approach (GoSam, FKS, VEGAS)
- Good parametrisation of phase space very important
- Mu3e cuts $E_{e^\pm} > 10 \text{ MeV}$, $|\cos \angle(\vec{p}_{e^\pm}, \vec{e}_z)| < 0.8$

Invisible energy spectrum



The angular distribution

- Distributions for the hard e^+ , soft e^+ and e^- with $E < 10$ MeV



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- Ready to compute “experiment-specific” observables

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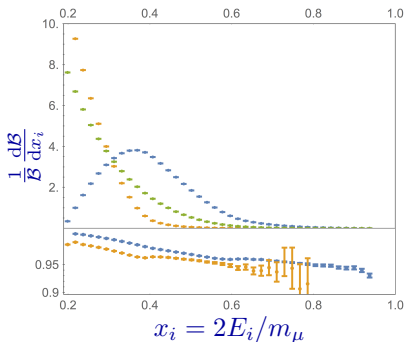
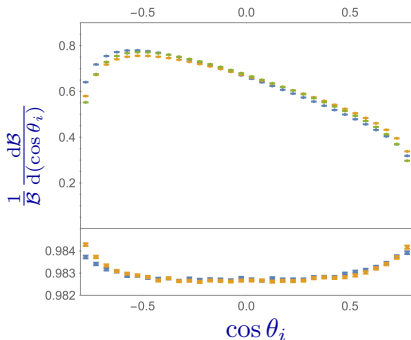
- Ready to compute “experiment-specific” observables
- Clarify role of real emissions



Backup slides

Flipping in angular distribution

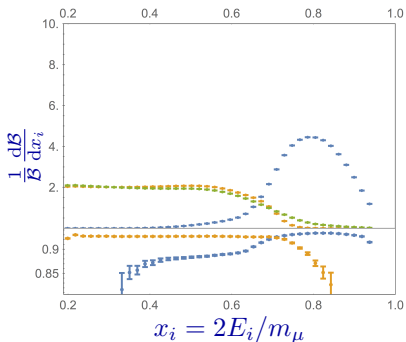
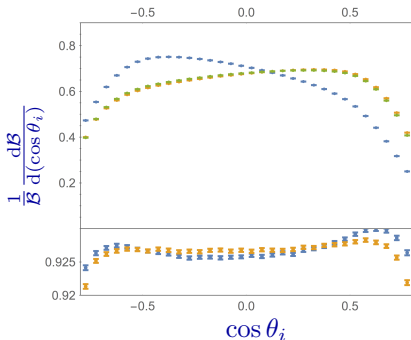
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No cut on \cancel{E}

Flipping in angular distribution

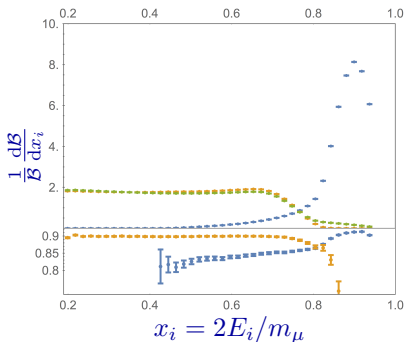
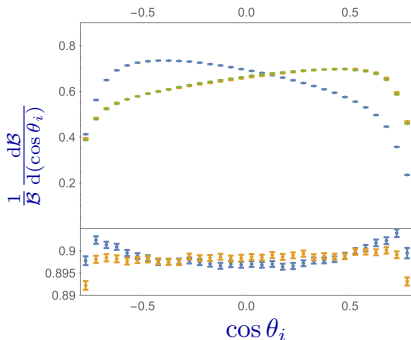
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$$E \leq 20 \text{ MeV}$$

Flipping in angular distribution

- Distributions for the hard e^+ , soft e^+ and e^-



$$E \leq 10 \text{ MeV}$$

- Two equivalent ways of introducing polarisations dependence

- “Closing the trace” $u(p)\bar{u}(p) = (\not{p} + m) \frac{1 + \gamma^5 \not{\epsilon}}{2}$
- Massive spinor helicity formalism

$$u_{\pm}(p) = \langle \ell^{\pm} | + \frac{m}{\langle \ell^{\pm} n^{\mp} \rangle} \langle n^{\mp} |$$

$$\ell = k - \frac{m^2}{2k \cdot n} n$$

Lightlike reference vector $n = (1, -\vec{s}/|\vec{s}|)$, combine

$$\mathcal{A} = \frac{1+|\vec{s}|}{2} \mathcal{A}^+ + \frac{1-|\vec{s}|}{2} \mathcal{A}^-$$

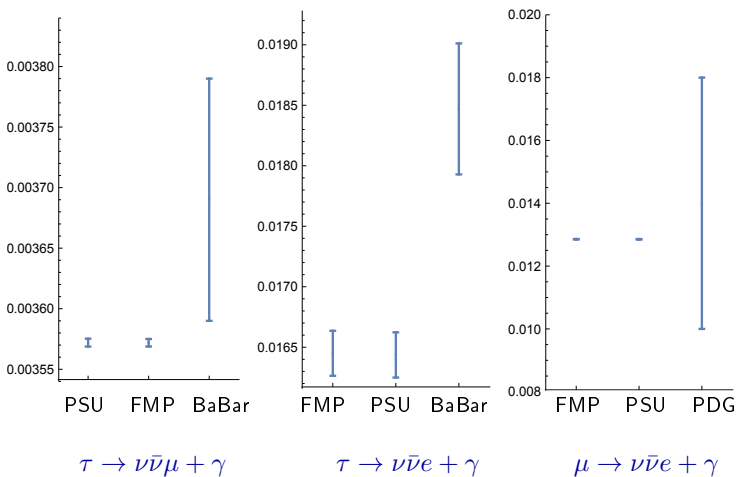
- Both introduce a γ^5 !

- $\gamma^5 = i\gamma^0\gamma^1\gamma^2\gamma^3$ is not well defined in d dimensions
- There are at two sources of γ^5 :
 - The 4-Fermi vertex $j_{V-A}^\mu(a, b) = \bar{\psi}_a\gamma^\mu(1 - \gamma^5)\psi_b$: [?]

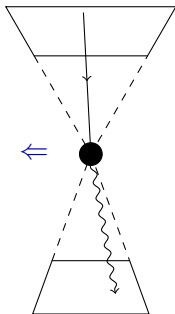
$$j_{V-A}^\mu(a, b) = \underbrace{\bar{\psi}_a\gamma^\mu\psi_b}_{j^\mu} - \bar{\psi}_a\gamma^\mu\psi'_b$$

- $\psi'_b = \gamma^5\psi_b$ corresponds to an electron with $m = -m_e$.
- Polarisation: Spinor helicity formalism in FDH (external particles in $d = 4$)

$$\delta\text{BR}^{\text{NNLO}} \approx \frac{\alpha}{\pi} \log \frac{m}{M} \log \frac{\omega_0}{M} \text{BR}^{\text{NLO}} \quad [?]$$



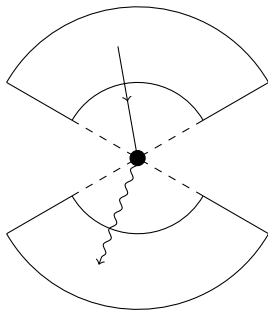
Theorist's version of the MEG detector @ PSI

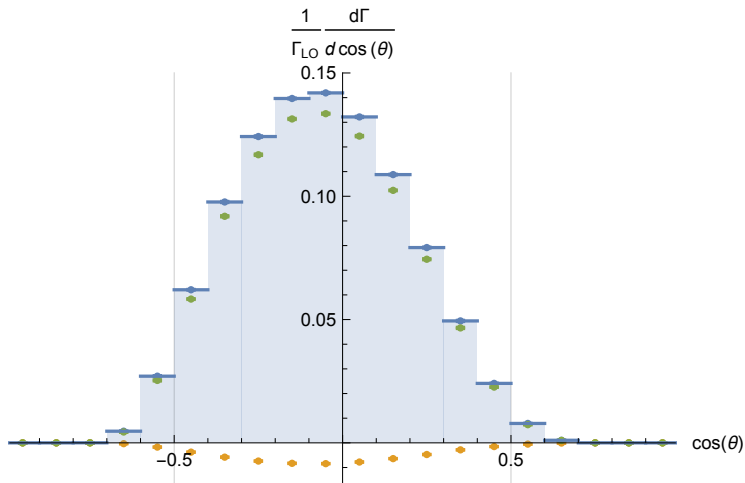


$$E_\gamma > 40 \text{ MeV}$$

$$|\cos \theta_e| < 0.5$$

$$E_e > 45 \text{ MeV}$$





MEG cuts on the electron loose **4.10%** of the events

- Standard (recursive): $p_1 \rightarrow p_2 + q \rightarrow p_2 + p_3 + q' \rightarrow \dots$
- Problem: Pseudo-singularities like $\frac{1}{(k+p)^2} \approx \frac{1}{\xi^2} \frac{1}{1-c_\theta+\epsilon(m_e)}$ are not aligned with VEGAS grid
- Idea: Parametrise energies and angles of “problematic” particles

